2016 James S. Rickards Fall Invitational

For all questions, answer choice (E) NOTA means that none of the given answers is correct. Good Luck!

1		ftf FL 10L	1 1519							
1.	ũ	mmon factor of $5!$, $10!$, an		(\mathbf{D})						
	(A) 25	(B) 50	(C) 120	(D) 3628800	(E) NOTA					
0	2. What is the smallest prime number that is 1 greater than a perfect square?									
Ζ.										
	(A) 5	(B) 2	(C) 7	(D) 17	(E) NOTA					
9										
3.	Solve for x in the follow (A) 1	ing equation. $7x + 13 = 2$ (B) 2	2x + 23 (C) 3	(D) 4	(E) NOTA					
	(11) 1	(\mathbf{D}) 2	(0) 0							
4	. Evaluate: $(1 + 2 + 3 + 4 + \ldots + 99 + 100)^0$									
ч.	(A) 5050	(B) 10100	(C) 1	(D) 0	(E) NOTA					
					、 ,					
5	5. If $a = \frac{b}{13} + 3$, what is <i>a</i> when <i>b</i> is 91?									
0.	(A) 7 $13 + 5$, what is a	(B) 13	(C) 20	(D) 3	(E) NOTA					
		(D) 10	(0) 20							
6	What is the slope of the line perpendicular to the one containing the points $(7, 13)$ and $(9, 14)$?									
0.		(B) 2	1	<u>`</u> 1´``	(E) NOTA					
	(A) -2	(D) 2	(C) $-\frac{1}{2}$	(D) $\frac{1}{2}$	(E) NOTA					
_	7. $\frac{1}{3}$ of $\frac{1}{2}$ of x is 10. What is the value of x?									
7.	$\frac{1}{3}$ of $\frac{1}{2}$ of x is 10. What	is the value of x ?								
	(A) 30^{-1}	(B) 45	(C) 10	(D) 60	(E) NOTA					
_										
8.	Oddish hates odd numb (A) 50	ers. How many 2-digit nu (B) 30	mbers only have odd digit (C) 49	ts? (D) 51	(E) NOTA					
	(A) 50	(D) 50	(0) 49	(D) 51	(E) NOTA					
0										
9.	9. Let x be the first positive integer that is a perfect power of 11 and not a palindrome. What is the sum of the dig of x ? (Hint: Use Pascal's triangle.)									
	(A) 11	(B) 32	(C) 14	(D) 22	(E) NOTA					
10.	What is the sum of the	distinct roots of the follow	ving equation? $(x-1)(x-1)$	$(x-3)(x-5)\dots(x-99) =$	0.					
	(A) 4950	(B) 100	(C) 10000	(D) 2550	(E) NOTA					
11.			ax can eat a doughnut in		work together,					
	(A) 9	(B) 20 (B) 20	All answers are in seconds (C) 36	.) (D) 18	(E) NOTA					
	(11) 0	(D) = 20	(0) 50	(D) 10						
19	2. Cydney is at the point $(7, 20)$ and is walking to the next PokeStop which is at the point $(18, 80)$. What									
12.		en Cydney and his destina		in is at the point (10,00)	. What is the					
	(A) 41	(B) 60	(C) 40	(D) 61	(E) NOTA					
13.		of x that satisfy $ 2x+1 $								
	(A) $x < 9$	(B) $x > -10$	(C) $x < 9$ or $x > -10$	(D) $x < 9$ and $x > -10$	(E) NOTA					
14.			e largest number of penci							
	(A) 13	(B) 17	(C) 3	(D) 5	(E) NOTA					

Designer is thinking of some lyrics for his new song but needs help because he can only speak cursive. How many 3 letter "words" can he make using the first 4 letters of the alphabet? (Letters can be repeated and the words do not have to mean anything. Ex: AAA is a word.)							
(A) 24	(B) 26	(C) 4	(D) 12	(E) NOTA			
	Pikachu loves food and prime numbers, especially ones over 100. What is the sum of the digits of the 3rd smallest prime number greater than 100?						
(A) 11	(B) 10	(C) 9	(D) 8	(E) NOTA			
The diameter of a circle is an integer. The area of the circle is between 100 and 120 square units. What is the number of units in the circle's diameter?							
(A) 10	(B) 11	(C) 12	(D) 13	(E) NOTA			
8. Find the sum of al	l integer(s) that make th	the inequality $14 < \frac{7x}{2} < 3$	21 true.				
(A) 15	(B) 10	(C) 6	(D) 5	(E) NOTA			
9. Calculate the circu (A) $4\sqrt{\pi}$	imference of a circle with (B) $2\sqrt{\pi}$	h area 4. (C) $4\pi^2$	(D) $2\pi^2$	(E) NOTA			
). Find the next term (A) 66	n in the sequence: 1, 2, 6 (B) 91	, 15, 31, 56. (C) 48	(D) 74	(E) NOTA			
	A number x is equal to the product of 7, 24 and 48. What is the smallest positive integer y such that the product xy is a perfect cube?						
(Å) 8064	(B) 588	(C) 294	(D) 1	(E) NOTA			
Shiv is building a fence so his cow Bessie can roam in peace. If Shiv wants to construct a fence with integral sid lengths, but only has 80 units of fencing material, what is the area of the largest plot of land that Shiv can mal for Bessie?							
(A) 39	(B) 399	(C) 1600	(D) 400	(E) NOTA			
 Find the sum of th (A) 4536 	ne positive factors of 2010 (B) 4535	3. (C) 6556	(D) 6552	(E) NOTA			
Ashish is lifting some heavy 5 pound dumbbells, but begins to pout when he realizes Sairam is lifting 6 pour dumbbells. Ashish begins using whey protein to beat Sairam in their next arm wrestling contest. How many gran should Ashish take every day if the recommended amount is the least common multiple of 6, 5, and 30? (Assum Ashish uses some common sense and only takes the recommended amount.)							
(A) 60	(B) 15	(C) 30	(D) 3	(E) NOTA			
Sri realizes he is lacking some common sense so he decides to ask the rainbow god for help. The rainbow god wi only help him if he can express 0.1777 as a fraction in simplest form. What is Sri's answer assuming he answer it correctly?							

him. How long will his shadow be in feet if he stands next to Teja at the same time of the day? (A) $\frac{7}{3}$ (B) $\frac{3}{7}$ (C) $\frac{4}{7}$ (D) $\frac{7}{4}$ (E) NOTA

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- 27. Let A be the set of positive integers from 1 to 100 inclusive. Vishnu loves the number 101 so he decides to make as many groups of 2 numbers from set A that sum to 101. What is the maximum number of groups he can make?
 (A) 50
 (B) 49
 (C) 48
 (D) 47
 (E) NOTA
- 28. Sairam has a crush on you and decides to ask you out with the word "PLEASE". How many ways can the letters in the word "PLEASE" be arranged?
 (A) 720
 (B) 120
 (C) 1080
 (D) 360
 (E) NOTA
- 29. Maathesh loves 90° angles. Find the equation of the line that passes through the point (20, 30) and is perpendicular to the line containing the points (11, 15) and (15, 23). (A) 2x + 3y = 130 (B) 2x + y = 70 (C) x + 2y = 80 (D) x - 2y = -40 (E) NOTA
- 30. Now that the day is almost over, Sri, Nihar, and Josh decide to drive a big white van around town passing out 30 stolen candies to children. Josh opens his eyes and notices that each candy is labeled with every digit of π to the right of the decimal point. Josh begins to draw right triangles in his mind and then also notices that the answer to this question is the 30th digit of π (to the right of the decimal point) multiplied by 3162656. The answer to this question can also be solved by computing $\left(\frac{2016}{288}\right) \cdot 2016 \cdot 2017$. (Hint: The first two digits of π to the right of the decimal point are 1 and 4.) (A) 27453804 (B) 28463904 (C) 28434014 (D) 27433904 (E) NOTA